

Daniel E. López-Fogliani 2009, Madrid.

***Gravitino Dark Matter in
The $\mu\nu$ SSM***

Very Well Known SUSY Models

The MSSM: Minimal content of fields

The NMSSM: *Solves a problem of naturalness in the MSSM: the μ problem*

Beyond the MSSM and NMSSM

Why?

Beyond the MSSM and NMSSM

Why?

⇒ Neutrino Physics

Super-Kamiokande 1998 → Neutrinos are massive

First evidence of particle physics beyond the SM, MSSM, NMSSM ...

Proposal for a new Minimal Supersymmetric Standard Model : The $\mu\nu$ SSM

We can use the sneutrino Right-Handed $\tilde{\nu}^c$ field to solve the μ -problem.

This motivate to postulate a New Supersymmetric Standard Model, with the minimal natural matter content and without μ -problem:

$$\lambda \tilde{\nu}^c H_1 H_2$$

$$\mu = \lambda \langle \tilde{\nu}^c \rangle$$

The μ from ν Supersymmetric Standard Model ($\mu\nu$ SSM)

L-F and Carlos Muñoz, *Phys. Rev. Lett. B* **97** (2006) 041801 [arXiv:hep-ph/0508297]

The Superpotential

$$W = \epsilon_{ab} \left(Y_u^{ij} \hat{H}_2^b \hat{Q}_i^a \hat{u}_j^c + Y_d^{ij} \hat{H}_1^a \hat{Q}_i^b \hat{d}_j^c + Y_e^{ij} \hat{H}_1^a \hat{L}_i^b \hat{e}_j^c + Y_\nu^{ij} \hat{H}_2^b \hat{L}_i^a \hat{\nu}_j^c \right) \\ - \epsilon_{ab} \lambda^i \hat{\nu}_i^c \hat{H}_1^a \hat{H}_2^b + \frac{1}{3} \kappa^{ijk} \hat{\nu}_i^c \hat{\nu}_j^c \hat{\nu}_k^c,$$

R-parity is explicitly broken

Soft Terms

$$\begin{aligned} -\mathcal{L}_{\text{soft}} &= m_{H_1}^2 H_1^{a*} H_1^a + m_{H_2}^2 H_2^{a*} H_2^a + (m_{\tilde{\nu}^c}^2)^{ij} \tilde{\nu}_i^{c*} \tilde{\nu}_j^c + \dots \\ &+ \left[\epsilon_{ab} (A_\nu Y_\nu)^{ij} H_2^b \tilde{L}_i^a \tilde{\nu}_j^c + \dots + \frac{1}{3} (A_\kappa \kappa)^{ijk} \tilde{\nu}_i^c \tilde{\nu}_j^c \tilde{\nu}_k^c + \text{H.c.} \right] \\ &- \frac{1}{2} \left(M_3 \tilde{\lambda}_3 \tilde{\lambda}_3 + M_2 \tilde{\lambda}_2 \tilde{\lambda}_2 + M_1 \tilde{\lambda}_1 \tilde{\lambda}_1 + \text{H.c.} \right) . \end{aligned}$$

Once the electroweak symmetry is spontaneously broken, the neutral scalars develop in general the following VEVs:

$$\langle H_1^0 \rangle = v_1 , \quad \langle H_2^0 \rangle = v_2 , \quad \langle \tilde{\nu}_i \rangle = \nu_i , \quad \langle \tilde{\nu}_i^c \rangle = \nu_i^c .$$

For one family of neutrinos the minimization condition are

$$\begin{aligned}
 & \frac{1}{4}(g_1^2 + g_2^2)(\nu^2 + v_1^2 - v_2^2)v_1 + \lambda^2 v_1 \left(\nu^{c2} + v_2^2 \right) + m_{H_1}^2 v_1 - \lambda \nu^c v_2 (\kappa \nu^c + A_\lambda) \\
 & \qquad \qquad \qquad - \lambda Y_\nu \nu \left(\nu^{c2} + v_2^2 \right) = 0, \\
 & -\frac{1}{4}(g_1^2 + g_2^2)(\nu^2 + v_1^2 - v_2^2)v_2 + \lambda^2 v_2 \left(\nu^{c2} + v_1^2 \right) + m_{H_2}^2 v_2 - \lambda \nu^c v_1 (\kappa \nu^c + A_\lambda) \\
 & \qquad \qquad \qquad + Y_\nu^2 v_2 \left(\nu^{c2} + \nu^2 \right) + Y_\nu \nu \left(-2\lambda v_1 v_2 + \kappa \nu^{c2} + A_\nu \nu^c \right) = 0, \\
 & \lambda^2 \left(v_1^2 + v_2^2 \right) \nu^c + 2\kappa^2 \nu^{c3} + m_{\tilde{\nu}^c}^2 \nu^c - 2\lambda \kappa v_1 v_2 \nu^c - \lambda A_\lambda v_1 v_2 + \kappa A_\kappa \nu^{c2} \\
 & \qquad \qquad \qquad + Y_\nu^2 \nu^c \left(v_2^2 + \nu^2 \right) + Y_\nu \nu \left(-2\lambda \nu^c v_1 + 2\kappa v_2 \nu^c + A_\nu v_2 \right) = 0, \\
 & \qquad \qquad \qquad \frac{1}{4}(\mathbf{g}_1^2 + \mathbf{g}_2^2)(\nu^2 + \mathbf{v}_1^2 - \mathbf{v}_2^2)\boldsymbol{\nu} + \mathbf{m}_{\tilde{\nu}}^2 \boldsymbol{\nu} \\
 & \qquad \qquad \qquad + \mathbf{Y}_\nu^2 \nu^{c2} \nu + \mathbf{Y}_\nu \left(-\lambda \nu^{c2} \mathbf{v}_1 - \lambda \mathbf{v}_2^2 \mathbf{v}_1 + \kappa \mathbf{v}_2 \nu^{c2} + \mathbf{A}_\nu \nu^c \mathbf{v}_2 \right) = 0.
 \end{aligned}$$

Observe that: $\nu \lesssim m_D$

The Neutralino-Neutrino mass matrix is:

$$\mathcal{M}_n = \begin{pmatrix} M & m \\ m^T & 0_{3 \times 3} \end{pmatrix},$$

$$M = \begin{pmatrix} M_1 & 0 & -Av_d & Av_u & 0 & 0 & 0 \\ 0 & M_2 & Bv_d & -Bv_u & 0 & 0 & 0 \\ -Av_d & Bv_d & 0 & -\lambda_i \nu_i^c & -\lambda_1 v_u & -\lambda_2 v_u & -\lambda_3 v_u \\ Av_u & -Bv_u & -\lambda_i \nu_i^c & 0 & -\lambda_1 v_d + Y_{\nu_{i1}} \nu_i & -\lambda_2 v_d + Y_{\nu_{i2}} \nu_i & -\lambda_3 v_d + Y_{\nu_{i3}} \nu_i \\ 0 & 0 & -\lambda_1 v_u & -\lambda_1 v_d + Y_{\nu_{i1}} \nu_i & 2\kappa_{11j} \nu_j^c & 2\kappa_{12j} \nu_j^c & 2\kappa_{13j} \nu_j^c \\ 0 & 0 & -\lambda_2 v_u & -\lambda_2 v_d + Y_{\nu_{i2}} \nu_i & 2\kappa_{21j} \nu_j^c & 2\kappa_{22j} \nu_j^c & 2\kappa_{23j} \nu_j^c \\ 0 & 0 & -\lambda_3 v_u & -\lambda_3 v_d + Y_{\nu_{i3}} \nu_i & 2\kappa_{31j} \nu_j^c & 2\kappa_{32j} \nu_j^c & 2\kappa_{33j} \nu_j^c \end{pmatrix},$$

where $A = \frac{G}{\sqrt{2}} \sin \theta_W$, $B = \frac{G}{\sqrt{2}} \cos \theta_W$, and

$$m^T = \begin{pmatrix} -\frac{g_1}{\sqrt{2}} \nu_1 & \frac{g_2}{\sqrt{2}} \nu_1 & 0 & Y_{\nu_{1i}} \nu_i^c & Y_{\nu_{11}} v_u & Y_{\nu_{12}} v_u & Y_{\nu_{13}} v_u \\ -\frac{g_1}{\sqrt{2}} \nu_2 & \frac{g_2}{\sqrt{2}} \nu_2 & 0 & Y_{\nu_{2i}} \nu_i^c & Y_{\nu_{21}} v_u & Y_{\nu_{22}} v_u & Y_{\nu_{23}} v_u \\ -\frac{g_1}{\sqrt{2}} \nu_3 & \frac{g_2}{\sqrt{2}} \nu_3 & 0 & Y_{\nu_{3i}} \nu_i^c & Y_{\nu_{31}} v_u & Y_{\nu_{32}} v_u & Y_{\nu_{33}} v_u \end{pmatrix}$$

From the previous matrix, neutrino masses are given effectively by a see saw TeV scale

In first approximation the light neutrinos mass matrix is:

$$M_\nu = m^T M^{-1} m$$

With neutrino masses of order $10^{-2} \text{ eV} = 10^{-11} \text{ GeV} \Rightarrow$

$$10^{-11} \text{ GeV} = \frac{Y_\nu^2 (10^2 \text{ GeV})^2}{10^3 \text{ GeV}} \rightarrow Y_\nu \sim 10^{-6}$$

$$Y_\nu H_2 L \nu^c$$

- Escudero, L-F, Muñoz, Ruiz de Austri, 08
 - Analysis of the parameter space: Viable regions
 - Spectrum, Higgs, masses for the neutralinos, etc.
- Ghosh, Roy, 09
 - Correct Neutrino physics: Solutions are found even with diagonal neutrinos
 - Decay of the lightest neutralino as LSP. Branching ratios show correlations with neutrino mixing angles, which can be tested at the LHC
- Barlt, Hirsch, Vicente, Liebler, Porod, 09
 - LHC phenomenology: The neutralino-LSP may decay within the detector.
- Fidalgo, L-F, Muñoz, Ruiz de Austri, 09
 - Neutrino Physics: Description of how see-saw works in the model. Description of how to find easy solutions.
 - SCPV included.

Effective Neutrino mass matrix

(Diagonal Yukawas for Neutrinos)

$$(m_{eff|real})_{ij} \simeq \frac{v_u^2}{6\kappa\nu^c} Y_{\nu_i} Y_{\nu_j} (1 - 3\delta_{ij}) - \frac{1}{2M_{eff}} \left[\nu_i \nu_j + \frac{v_d (Y_{\nu_i} \nu_j + Y_{\nu_j} \nu_i)}{3\lambda} + \frac{Y_{\nu_i} Y_{\nu_j} v_d^2}{9\lambda^2} \right]$$

$$M_{eff} \equiv M \left[1 - \frac{v^2}{2M (\kappa\nu^{c^2} + \lambda v_u v_d)} \frac{1}{3\lambda\nu^c} \left(2\kappa\nu^{c^2} \frac{v_u v_d}{v^2} + \frac{\lambda v^2}{2} \right) \right] \quad \frac{1}{M} = \frac{g_1^2}{M_1} + \frac{g_2^2}{M_2}$$

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$$v_d \rightarrow 0 \quad (m_{eff|real})_{ij} \simeq \frac{v_u^2}{6\kappa\nu^c} Y_{\nu_i} Y_{\nu_j} (1 - 3\delta_{ij}) - \frac{1}{2M_{eff}} \nu_i \nu_j$$

or $\nu_i \gg \frac{Y_{\nu_i} v_d}{3\lambda}$

$$M_{eff} = M \left(1 - \frac{v^4}{12\kappa M \nu^c^3} \right)$$

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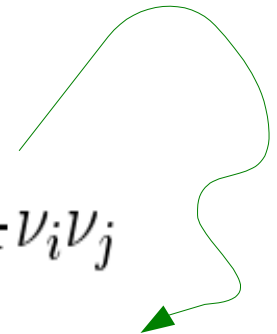
$$\begin{aligned} v_d &\rightarrow 0 \\ M_{eff} &\approx M \end{aligned} \quad (m_{eff|real})_{ij} \simeq \frac{v_u^2}{6\kappa\nu^c} Y_{\nu_i} Y_{\nu_j} (1 - 3\delta_{ij}) - \frac{1}{2M} \nu_i \nu_j$$

Effective Neutrino mass matrix

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Gaugino see saw

Effective Neutrino mass matrix

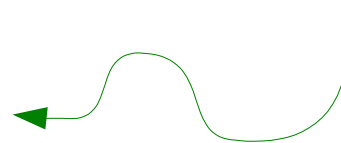
(Diagonal Yukawas for Neutrinos)

$$(m_{eff|real})_{ij} \simeq \frac{v_u^2}{6\kappa\nu^c} Y_{\nu_i} Y_{\nu_j} (1 - 3\delta_{ij}) - \frac{1}{2M_{eff}} \left[\nu_i \nu_j + \frac{v_d (Y_{\nu_i} \nu_j + Y_{\nu_j} \nu_i)}{3\lambda} + \frac{Y_{\nu_i} Y_{\nu_j} v_d^2}{9\lambda^2} \right]$$

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ν_R -Higgsino see saw



Then also with diagonal Yukawas for neutrinos the mixtures could be generated

In particular in the: ν_μ - ν_τ degenerate case.

$$m_{eff} = \begin{pmatrix} d & c & c \\ c & A & B \\ c & B & A \end{pmatrix}$$

$$\sin^2 \theta_{13} = 0$$

$$\sin^2 \theta_{23} = \frac{1}{2}$$

$$c = A + B - d \quad \longrightarrow \quad \sin^2 \theta_{12} = 1/3$$

Then close to the ν_μ - ν_τ degenerate case. and $c \approx A + B - d$

$$\sin^2 \theta_{23} \approx \frac{1}{2}, \quad \sin^2 \theta_{13} \approx 0, \quad \sin^2 \theta_{12} \approx 1/3$$

If we start at GUT scale with diagonal Yukawas for quarks and neutrinos we will obtain small off-diagonal Yukawas at low scale.

**In the quark sector this gives small mixing angles
but not in the neutrino sector.**

If we start at GUT scale with diagonal Yukawas for quarks and neutrinos we will obtain small off-diagonal Yukawas at low scale.

In the quark sector this gives small mixing angles but not in the neutrino sector.

**In some sense we have an explanation of :
Why the two sectors are so different?**

- Charginos mix with charged leptons

$$\Psi^{+T} = (-i\tilde{\lambda}^+, \tilde{H}_u^+, e_R^+, \mu_R^+, \tau_R^+)$$

$$\Psi^{-T} = (-i\tilde{\lambda}^-, \tilde{H}_d^-, e_L^-, \mu_L^-, \tau_L^-)$$

$$-\frac{1}{2}(\psi^{+T}, \psi^{-T}) \begin{pmatrix} 0 & M_C^T \\ M_C & 0 \end{pmatrix} \begin{pmatrix} \psi^{+T} \\ \psi^{-T} \end{pmatrix}$$

$$M_C = \begin{pmatrix} M_2 & g_2 v_u & 0 & 0 & 0 \\ g_2 v_d & \lambda_i \nu_i^c & -Y_{e_{i1}} \nu_i & -Y_{e_{i2}} \nu_i & -Y_{e_{i3}} \nu_i \\ g_2 \nu_1 & -Y_{\nu_{1i}} \nu_i^c & Y_{e_{11}} v_d & Y_{e_{12}} v_d & Y_{e_{13}} v_d \\ g_2 \nu_2 & -Y_{\nu_{2i}} \nu_i^c & Y_{e_{21}} v_d & Y_{e_{22}} v_d & Y_{e_{23}} v_d \\ g_2 \nu_3 & -Y_{\nu_{3i}} \nu_i^c & Y_{e_{31}} v_d & Y_{e_{32}} v_d & Y_{e_{33}} v_d \end{pmatrix}$$

- Neutral Higgs mix with sneutrinos
- Charged Higgs mix with charged sleptons

SUSY renormalizable theory: $\mu\nu$ SSM

$$M_{\text{SUSY}} \sim 1 \text{ TeV}$$

All known particles (including
neutrinos) + SUSY partners

Dark Matter ???

LSP is not stable

Neutralino is not a Dark Matter candidate

Also sneutrino (with right-handed component) it is not

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But

Dark Matter ???

LSP is not stable

Neutralino is not a Dark Matter candidate

Also sneutrino (with right-handed component) it is not

But

Neutralino has an important role in the
SUSY see-saw
(without imposing R parity)

Also sneutrino Right handed as part of the Higgs —→ important role

What about Dark matter???

What about Dark matter???

The only confirmed indications that Dark Matter exist are gravitational

SUSY

$\mu\nu$ SSM

$M_{\text{SUSY}} \sim 1 \text{ TeV}$

(Renormalizable)

Gravity ($G_{\mu\nu}$)

(Non Renormalizable)

$$M_{\text{Planck}} \sim 10^{16} \text{ TeV}$$

SUSY

$\mu\nu$ SSM

$$M_{\text{SUSY}} \sim 1 \text{ TeV}$$

(Renormalizable)

SUGRA (local SUSY)

$$(G_{\mu\nu}, \Psi_{\mu})$$

(graviton, gravitino)

$$M_{\text{Planck}} \sim 10^{16} \text{ TeV}$$

(Non Renormalizable)

Tree level amplitudes

SUSY

$\mu\nu$ SSM

$$M_{\text{SUSY}} \sim 1 \text{ TeV}$$

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Tree level amplitudes

SUSY

$\mu\nu$ SSM

$$M_{\text{SUSY}} \sim 1 \text{ TeV}$$

(Renormalizable)

Similar as in a Fermi theory where

$$G_F \sim 1/M_W^2$$

Gravitino: Could be Dark matter

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Direct detection: Not possible 😞

Gravitino: Could be Dark matter

Direct detection: Not possible 😞

Indirect detection: In principle possible !!! 😊

Tree level interactions

Takayama, Yamaguchi, 2000

gravitino-photon-photino (λ):

$$L_{int} = -\frac{i}{8M_{pl}} \bar{\psi}_\mu [\gamma^\nu, \gamma^\rho] \gamma^\mu \lambda F_{\nu\rho},$$

$$\Gamma(\Psi_{3/2} \rightarrow \sum_i \gamma \nu_i) \simeq \frac{1}{32\pi} |U_{\tilde{\gamma}\nu}|^2 \frac{m_{3/2}^3}{M_P^2},$$

Lifetime of the gravitino can be longer than the age of the Universe ($\sim 10^{17}$ s)

$$\tau_{3/2} = \Gamma^{-1}(\tilde{G} \rightarrow \gamma \nu) \simeq 8.3 \times 10^{26} \text{ sec} \times \left(\frac{m_{3/2}}{1 \text{ GeV}} \right)^{-3} \left(\frac{|U_{\gamma\nu}|^2}{7 \times 10^{-13}} \right)^{-1}.$$

Relic density

$$\Omega_{3/2} h^2 \simeq 0.27 \left(\frac{T_R}{10^{10} \text{ GeV}} \right) \left(\frac{100 \text{ GeV}}{m_{3/2}} \right) \left(\frac{m_{\tilde{g}}}{1 \text{ TeV}} \right)^2$$

$$\Omega_{3/2} h^2 \simeq 0.1 \text{ for } T_R \sim 10^8 - 10^{11} \text{ GeV, with } m_{\tilde{g}} \sim 1 \text{ TeV}$$

DETECTION

- ❖ Decays of **gravitinos** in the galactic halo, at a sufficiently high rate, would produce gamma rays that could be detectable in future experiments

An experiment such as **FERMI**, launched last year, might in principle detect these gamma rays

Buchmuller, Covi, Hamaguchi, Ibarra, Yanagida, 2007

Bertone, Buchmuller, Covi, Ibarra, 2007

Ibarra, Tran, 2008

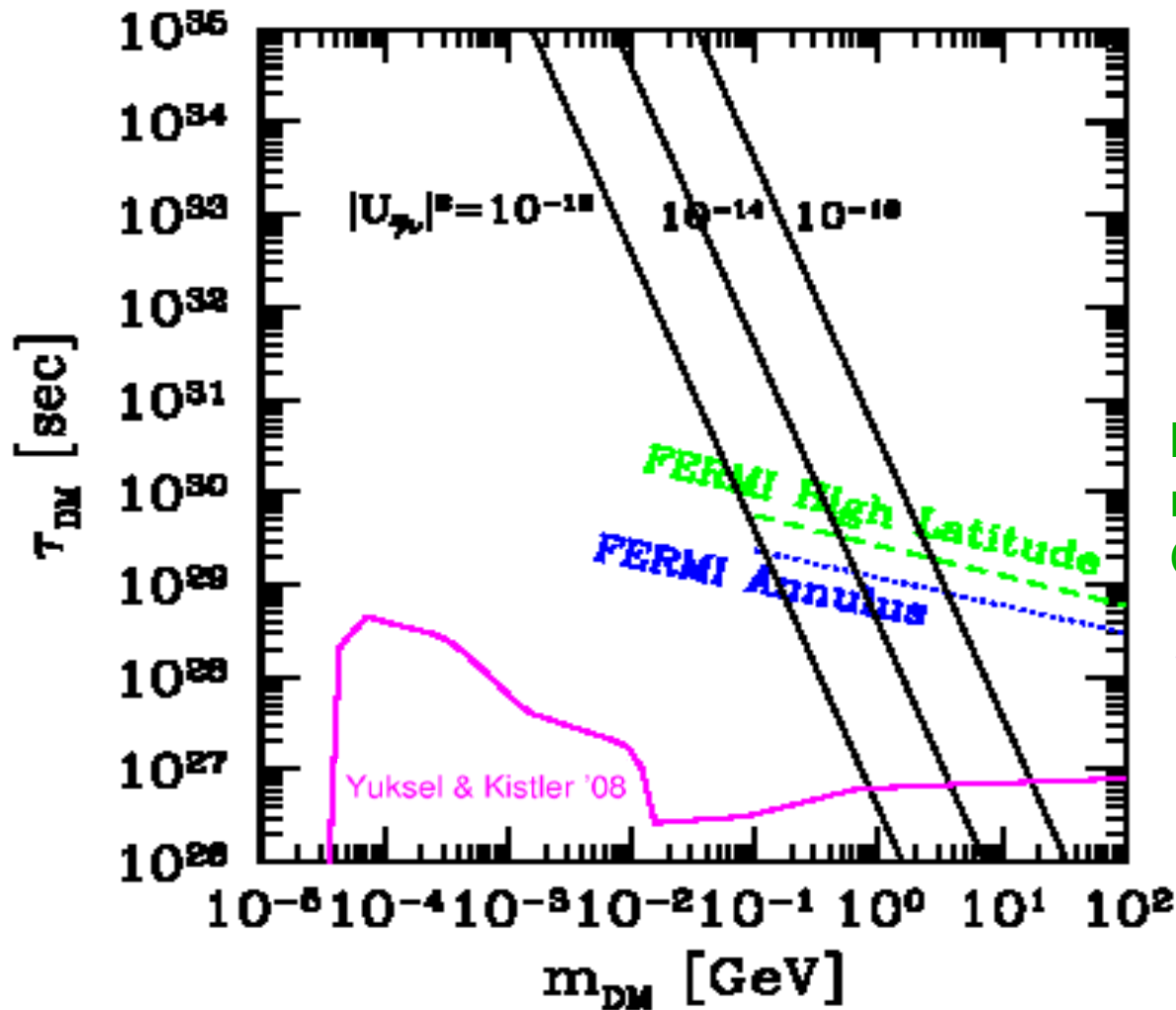


$$\left[E^2 \frac{dJ}{dE} \right]_{\text{halo}} = \frac{2E^2}{m_{3/2}} \frac{dN_\gamma}{dE} \frac{1}{8\pi\tau_{3/2}} \int_{\text{los}} \rho_{\text{halo}}(\vec{l}) d\vec{l},$$

The integration extends over the line of sight implying an angular dependence on the direction of observation. This produces an anisotropic gamma ray flux

Since the gravitino decays into a photon and neutrino, this produces two monochromatic lines at energies equal to $m_{3/2}/2$

Indirect detection

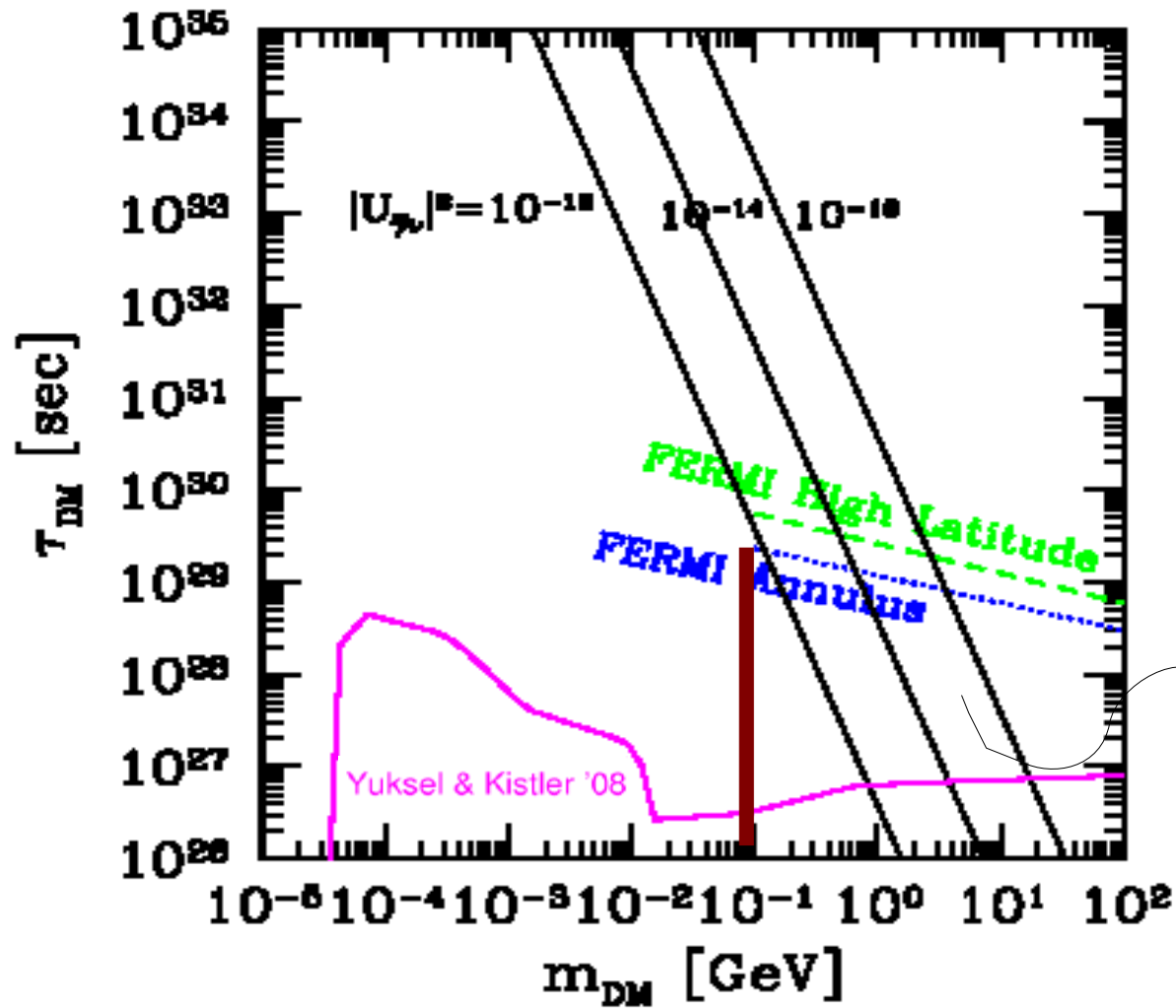


$$U \sim g_1 v/M_1 \sim 10^{-6} - 10^{-8}$$

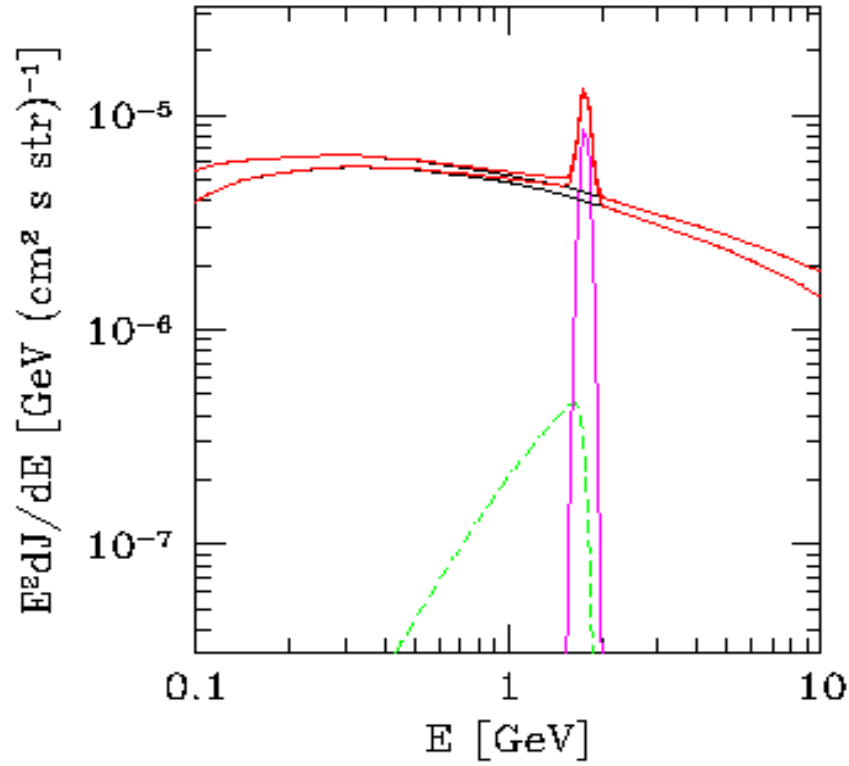
latitude $>20^\circ$ but excluding the region within 35° of the Galactic Center

within 25° to 35° of Galactic Center but excluding $\pm 10^\circ$ of the Galactic equator

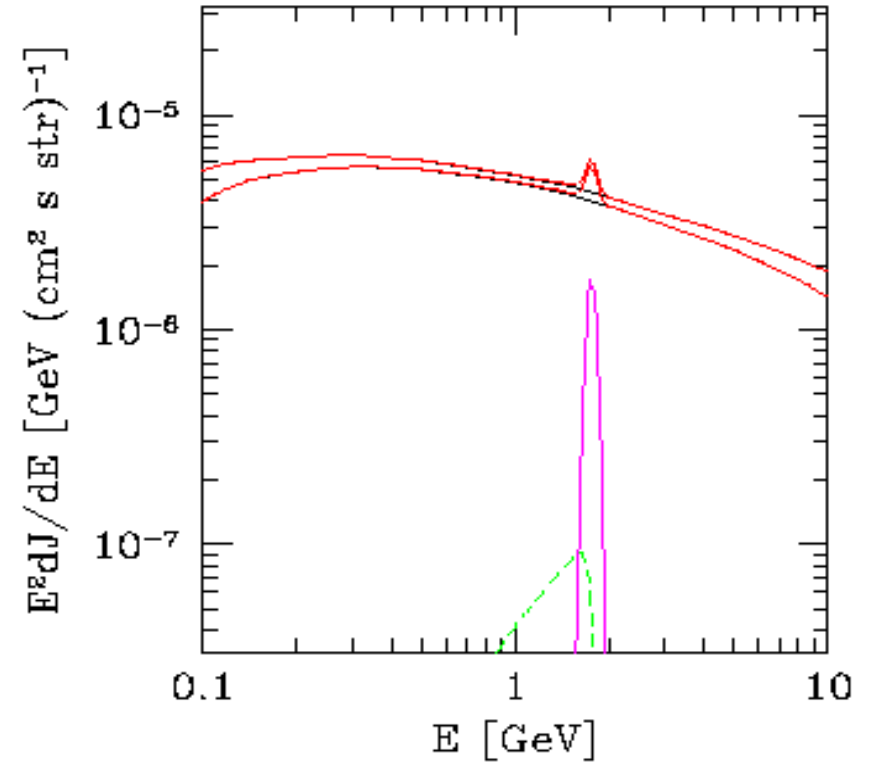
Indirect detection



Observable



(a)



(b)

Figure . Expected gamma-ray spectrum for an example of gravitino dark matter decay in the mid-latitude range ($10^\circ \leq |b| \leq 20^\circ$) in the $\mu\nu$ SSM with $m_{3/2} = 3.5$ GeV and (a) $|U_{\tilde{\gamma}\nu}|^2 = 8.8 \times 10^{-15}$ corresponding to $\tau_{3/2} = 10^{27}$ s, (b) $|U_{\tilde{\gamma}\nu}|^2 = 1.7 \times 10^{-15}$ corresponding to $\tau_{3/2} = 5 \times 10^{27}$ s. The green dashed, magenta solid, and black solid lines correspond to the diffuse extragalactic gamma ray flux, the gamma-ray flux from the halo, and to the conventional background. respectively. The total gamma-ray flux is shown with red solid lines.

Conclusion

- ① **Very Rich** and different **Phenomenology** from MSSM/NMSSM
- ② We used the **right-handed sneutrino field** to solve the μ -problem of the MSSM without introducing an extra field as in the NMSSM
- ③ We include **Neutrino Physics** in a very natural way.
Renormalizable theory with the **minimal content of matter** (with tree level masses for the three neutrinos) only one scale M_{SUSY}
- ④ After EW symmetry breaking $\rightarrow$ **see saw mechanism at EW scale**
R parity is broken $\rightarrow$ **Neutralino important roll** in the see saw
- ⑤ **Gravitino** is the supersymmetric partner of graviton,
(in a local SUSY theory, Non-Renormalizable, is part of the spectrum)
 $\rightarrow$ **could be Dark Matter**, and might be tested

RGEs

$$\frac{d}{dt}\kappa_{ijk} = \frac{1}{16\pi^2}(\kappa_{ljk}\gamma_{\nu_i^c}^{\nu_l^c} + \kappa_{lik}\gamma_{\nu_j^c}^{\nu_l^c} + \kappa_{lji}\gamma_{\nu_k^c}^{\nu_l^c}) ,$$

$$\frac{d}{dt}\lambda_i = \frac{1}{16\pi^2}(\lambda_j\gamma_{\nu_i^c}^{\nu_j^c} + \lambda_i\gamma_{H_u}^{H_u} + \lambda_i\gamma_{H_d}^{H_d}) + \frac{1}{16\pi^2}Y_{\nu ji}\gamma_{H_d}^{L_j} ,$$

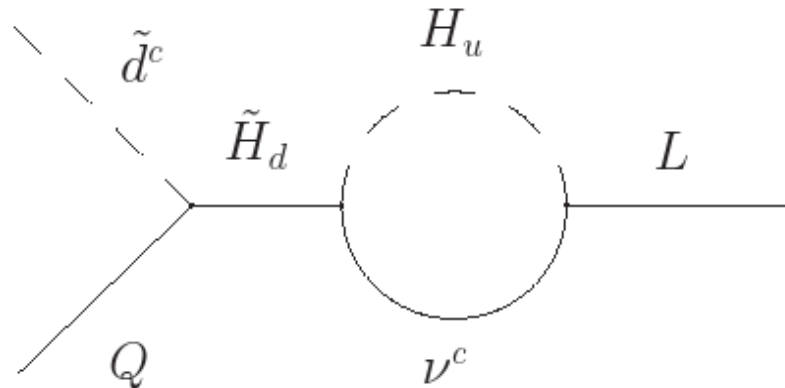
$$\frac{d}{dt}Y_{\nu ij} = \frac{1}{16\pi^2}(Y_{\nu ij}\gamma_{H_u}^{H_u} + Y_{\nu ik}\gamma_{\nu_j^c}^{\nu_k^c} + Y_{\nu kj}\gamma_{L_i}^{L_k}) + \frac{1}{16\pi^2}\lambda_j\gamma_{L_i}^{H_d} ,$$

$$\frac{d}{dt}Y_{eij} = \frac{1}{16\pi^2}(Y_{eij}\gamma_{H_d}^{H_d} + Y_{eik}\gamma_{e_j^c}^{e_k^c} + Y_{eik}\gamma_{L_j}^{L_k}) ,$$

$$\frac{d}{dt}Y_{dij} = \frac{1}{16\pi^2}(Y_{dij}\gamma_{d_j^c}^{d_k^c} + Y_{d_{kj}}\gamma_{Q_i}^{Q_k} + Y_{d_{ij}}\gamma_{H_d}^{H_d}) ,$$

$$\frac{d}{dt}Y_{uij} = \frac{1}{16\pi^2}(Y_{uik}\gamma_{u_j^c}^{u_k^c} + Y_{u_{kj}}\gamma_{Q_i}^{Q_k} + Y_{u_{ij}}\gamma_{H_u}^{H_u}) ,$$

$$\frac{d}{dt}\lambda'_{ijk} = \frac{1}{16\pi^2}Y_{d_{jk}}\gamma_{L_i}^{H_d} .$$



$$\gamma_{\nu_i^c}^{\nu_j^c} = -2(\kappa_{ilk}\kappa_{jlk} + \lambda_i\lambda_j + Y_{\nu_{ki}}Y_{\nu_{kj}}) ,$$

$$\gamma_{H_u}^{H_u} = \frac{3}{2}g_2^2 + \frac{3}{10}g_1^2 - 3Y_{u_{ij}}Y_{u_{ij}} - \lambda_i\lambda_i - Y_{\nu_{ij}}Y_{\nu_{ij}} ,$$

$$\gamma_{H_d}^{H_d} = \frac{3}{2}g_2^2 + \frac{3}{10}g_1^2 - Y_{e_{ij}}Y_{e_{ij}} - 3Y_{d_{ij}}Y_{d_{ij}} - \lambda_i\lambda_i ,$$

$$\gamma_{L_i}^{L_j} = \frac{3}{2}g_2^2 + \frac{3}{10}g_1^2 - Y_{e_{ik}}Y_{e_{jk}} - Y_{\nu_{il}}Y_{\nu_{jl}} ,$$

$$\gamma_{L_i}^{H_d} = \gamma_{H_d}^{L_i} = -Y_{\nu_{ij}}\lambda_j ,$$

$$\gamma_{e_i^c}^{e_j^c} = \frac{6}{5}g_1^2 - 2Y_{e_{ik}}Y_{e_{jk}} ,$$

$$\gamma_{d_i^c}^{d_j^c} = \frac{8}{3}g_s^2 + \frac{2}{15}g_1^2 - 2Y_{d_{ik}}Y_{d_{jk}} ,$$

$$\gamma_{u_i^c}^{u_j^c} = \frac{8}{3}g_s^2 + \frac{8}{15}g_1^2 - 2Y_{u_{ik}}Y_{u_{jk}} ,$$

$$\gamma_{Q_i}^{Q_j} = \frac{8}{3}g_s^2 + \frac{3}{2}g_2^2 + \frac{1}{30}g_1^2 - Y_{u_{ik}}Y_{u_{jk}} - Y_{d_{ik}}Y_{d_{jk}} ,$$